Mathematics and the second sec

Edexcel IAL

51

Worksheet Answers

Measures of Location and Spread

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Mathematical Modelling:

Exercise:

- 1 The statistical tests provide a clear and objective means of deciding the differences between the model's prediction and experimental data. These tests will show if and how the model can be refined even further.
- 2 Predictions based on the model are compared with the experimental data. By analysing this, the model and is adjusted and refined. The process is repeated.
- 3 Stage 1: The recognition of a real-world problem
 - Stage 4: Experimental data is collected from the real world
 - Stage 6: Statistical concepts are used to test how well the model describes the real-world problem

Measures of Location and Spread

Exercise 1:

- 1 a Quantitative as it is numerical
 - b Qualitative as it is a descriptive word
 - c Quantitative as it is numerical
 - d Ouantitative as it is numerical
 - e Qualitative as it is a descriptive word
- 2 a Not True
- **b** True

c True

- d Not True
- **3 a** 5.95 and 6.95
- **b** 9.45
- 4 a 1.4 and 1.5
- **b** 1.35

Exercise 2:

- 1 a 700 g
- **b** 600 g
- d The mean will increase; the mode will remain unchanged; the median will decrease.
- 2 a 42.7
 - **b** The mean will increase.
- 3 a May: 23 355 m, June: 21 067 m
 - **b** 22 230 m
- 4 a 8 minutes
- **b** 10.2 minutes **c** 8.5 minutes
- d The median would be best. The mean is affected by the extreme value 26.
- 5 a 2
- **b** 1
- c 1.47
- d the median

- **6** 6.31 petals
- 7 p = 1

Exercise 3:

- 1 a €351 to €400
- **b** €345 **c** €351 to €400
- 2 a 82.3 decibels
 - b The mean is an estimate as we don't know the exact noise levels recorded.
- 3 a $16 \le t < 18$
 - **b** 16.5 °C (correct to 3 s.f.)
- 4 Shop B (mean 51 years) employs older workers than shop A (mean 50 years).

Exercise 4:

1 a 1020 hPa **b** $Q_1 = 1017 \text{ hPa}, Q_3 = 1024.5 \text{ hPa}$

2 $Q_1 = 37$, $Q_2 = 37$, $Q_3 = 38$

3 1.08

4 a 432 kg **b** 389 kg **c** 480 kg

d Three-quarters of the cows weigh 480 kg or less.

5 a 44.0 minutes **b** 48.8 minutes

c 90th percentile = 57.8 minutes so 10% of customers have to wait longer 57.8 minutes, not 56 minutes as stated by the firm.

6 a 2.84 m. 80% of condors have a wingspan of less than 2.84 m.

b The 90th percentile is in the $3.0 \le w$ class. There is no upper boundary for this class, so it is not possible to estimate the 90th percentile.

Exercise 5:

1 a 71 **b** 24.6 **c** 193.1 mm **d** 7

2 a \$81.87 **b** 22

h 54

3 a 6.2 minutes **b** 54

4 a Median 11.5 °C, $Q_1 = 10.3$ °C, $Q_3 = 12.7$ °C, IQR = 2.4 °C

b On average, the temperature was higher in June than in May (higher median). The temperature was more variable in May than June (higher IQR).

c 24 days

Exercise 6:

1 a 3 **b** 0.75 **c** 0.866

2 3.11 kg

3 a $178 \,\mathrm{cm}$ b $59.9 \,\mathrm{cm}^2$ c $7.74 \,\mathrm{cm}$

4 Mean 5.44, standard deviation 2.35

5 a Mean OMR10.22, standard deviation OMR1.35

b 19

6 1.23 days

- 7 Mean 16.1 hours, standard deviation 4.69 hours One standard deviation below mean 11.41 hours. 41 parts tested (82%) lasted longer than one standard deviation below the mean. According to the manufacturers, this should be 45 parts (90%), so the claim is false.
- 8 a Mean 8.1 knots, standard deviation 3.41 knots
 - **b** 12 days
 - c The wind speeds are equally distributed throughout the range.

Challenge

Mean = 81.8 cents, standard deviation = \$1.03

Exercise 7

- **1** a 11, 9, 5, 8, 3, 7, 6
- **b** 7
- **c** 70
- **2 a** 7, 10, 4, 10, 5, 11, 2, 3 **b** 6.5
- c 48.5

- **3** 365
- 4 2.34
- 5 a

Battery life (b years)	Frequency (f)	Midpoint (x)	$y = \frac{x - 14}{2}$
11-21	11	16	1
21–27	24	24	5
27-31	27	29	7.5
31-37	26	34	10
37-43	12	40	13

b Coded mean = 7.495

Actual mean - 28.99 or 29 hours to the nearest hour

- **6 a** 1.2 hours
- **b** 25.1 hours **c** 1.76 hours

- 7 22.9
- 8 416 mm
- 9 Mean 1020 hPa, standard deviation 6.28 hPa